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ZBW – Leibniz-Informationszentrum Wirtschaft/Leibniz Information Centre for Economics Düsternbrooker Weg 120 24105 Kiel (Germany) E-Mail: rights[at]zbw.eu https://www.zbw.eu/econis-archiv/

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New directions in measurement of economic growth, development and under development

By Mario COCCIA †

Abstract. This paper presents a simple model to measure the relative economic growth of economic systems. The model considers S-Shaped patterns of economic growth that, represented with a linear model, measure how an economic system grows in comparison with another one. In particular, this model introduces an approach which indicates if the economic system has a process of economic growth, development or underdevelopment. The application of the model is provided for regions and macro regions of the Italian economic system.

Keywords. Economic growth, Convergence, Economic development, Relative growth, *S*-shaped pattern.

JEL. C02, F43, O40, O47.

1. Introduction

et Y(t) be the total output at time t of the economic system Y' and X(t) be the total output at the same time of the economic system X'; let $Y'\supseteq X'$, b_1 and b_2 be the rates of growth of total outputs Y and X, respectively, such that $B_1 = \frac{b_2}{b_1}$; if Y and X increase, in the long run, according to some S-shaped

pattern of growth, then $B_1 = \frac{b_2}{b_1}$ measures the relative economic growth of the

economic system X' in relation to the economic growth Y'.

In fact, if both Y and X increase in the long run according to some S-shaped pattern of growth (Lewis, 1955; Jarne *et al.*, 2005), one way to represent such a pattern formally is in terms of the differential equation of the well-known logistic function. In the case of Y(t) we have:

$$\frac{1}{Y}\frac{dY}{dt} = \frac{b_1}{K_1}(K_1 - Y)$$

This equation can be rewritten as

$$\frac{K_1}{Y} \frac{1}{(K_1 - Y)} dY = b_1 dt \frac{dY}{Y} - \frac{-dY}{(K_1 - Y)} = b_1 dt$$

Upon integrating we obtain

^{4†} Arizona State University, Interdisciplinary Science and Technology Building 1 (ISBT1) 550 E. Orange Street, Tempe- AZ 85287-4804 USA.

². + 85287-4804

[.] mario.coccia@cnr.it

$$\log Y - \log(K_1 - Y) = A_1 + b_1 t$$

$$\log \frac{K_1 - Y}{Y} = a_1 - b_1 dt$$

$$Y = \frac{K_1}{1 + \exp(a_1 - b_1 t)}$$

where $a_1 = b_1 dt$, and t_i is the abscissa of the point of inflection. Thus the growth of Y and X can be described as:

$$\log \frac{K_1 - Y}{Y} = a_1 - b_1 t \tag{1}$$

for X(t) we proceed in similar way of Y(t) and we have:

$$\log \frac{K_2 - X}{X} = a_2 - b_2 t \tag{2}$$

respectively.

It can be readily verified that the logistic curve is a symmetrical S-shaped curve with a point of inflection at $0.5K^1$

Solving the equations (1) and (2) for t,

$$t = \frac{a_1}{b_1} - \frac{1}{b_1} \log \frac{K_1 - Y}{Y} = \frac{a_2}{b_2} - \frac{1}{b_2} \log \frac{K_2 - X}{X}$$

which immediately yields the expression

$$\frac{Y}{K_1 - Y} = C_1 \left(\frac{X}{K_2 - X}\right)^{\frac{b_1}{b_2}} \tag{3}$$

Clearly:

$$C_1 = \exp\left(\frac{a_2b_1 - a_1b_2}{b_2}\right)$$
, which can be written in a simplified form as

 $C_1 = \exp[b_1(t_2 - t_1)]$ since, as noted earlier, $a_1 = b_1t_1$ and $a_2 = b_2t_2$ (cf. Eqs. (1) and (2)).

When X and Y are small in comparison with their final value, Eq. (3) reduces to

$$\frac{Y}{K_1} = C_1 \left(\frac{X}{K_2}\right)^{\frac{b_1}{b_2}}$$

¹ Briefly, a_1 is a constant depending on the initial conditions, K_1 is the equilibrium level of growth, and b_1 is the rate-of-growth parameter.

Hence the following simple model of economic growth is obtained

$$X = A_1(Y)^{B_1} \tag{4}$$

where
$$A_1 = \frac{K_2}{(K_1)^{\frac{b_2}{b_1}}} C_1$$
 and $B_1 = \frac{b_2}{b_1}$

The Eq. (4) was used by Huxley (1932) to describe the shape changes which animals and plans undergo during growth. In similar way this allometry equation [4] can be used to describe the changes of economic systems undergo during economic growth. The standard approach his to submit relative growth data to a logarithmic transformation before carrying out calculations. In fact, the logarithmic form of the equation $X = A_1(Y)^{B_1}$ is a simple linear relationship,

$$\log X = \log A_1 + B_1 \log Y$$

 B_1 is the allometry exponent of the X relatively to the Y. If the relative growth of the two dimensions were *isometric* (i.e. it produces economic growth), the allometry exponent B_1 should have a unit value. This hypothesis is expressed as:

$$B_{1} = 1$$

On the other hand, the hypothesis that X increases at greater relative rate that Y, the hypothesis of positive allometric growth or economic development, could be expressed as:

$$B_1 > 1$$

the hypothesis that X a negative allometric growth (under development) relatively to Y would be expressed as:

$$B_1 < 1$$

Remark: Gompertz function

It is not necessary that the growth curves of economic system be of the logistic form. For instance, suppose that the pattern of economic growth is described as a Gompertz function:

$$\frac{1}{Y}\frac{dY}{dt} = J_1 \exp(I_1 - J_1 t)$$

The integral form of this equation is:

$$\log Y = -\exp(I_1)\exp(-J_1t) + \log K_1$$

or
$$Y = K_1 \exp\left[-\exp\left(I_1 - J_1 t\right)\right]$$

Thus the growth of Y and X can be described as:

$$\log\log\frac{K_1}{Y} = I_1 - J_1 t \tag{5}$$

$$\log\log\frac{K_2}{Y} = I_2 - J_2 t \tag{6}$$

This equation represents the Gompertz type of economic growth process and unlike the logistic, the Gompertz curve² is an asymmetrical S-shaped curve with a point of inflection at Y = K/e of the limit to growth.

Solving the equations (5) and (6) for t, we have

$$t = -\frac{1}{J_1} \left(\log \log \frac{K_1}{Y} - I_1 \right) = -\frac{1}{J_2} \left(\log \log \frac{K_2}{X} - I_2 \right)$$
or
$$\log \log \frac{K_1}{Y} = \log M + \log \left(\log \frac{K_2}{X} \right)^{\nu}$$
(7)

where:

$$v = \frac{J_1}{J_2}$$
, $M = \frac{G_1}{G_2^v}$, $G_1 = e^{I_1}$, $G_2 = e^{I_2}$; solving for Y , we have $Y = K_1 \exp \left[-M \left(\log \frac{K_2}{X} \right)^v \right]$

If both variables under consideration grow at the same rate, that is, v=1, then

$$Y = \left(\frac{K_1}{K_2^M}\right) X^M \tag{8}$$

Further, $M = \frac{e^{I_1}}{e^{I_2}}$, since v=I. Thus the value of M depends only on two constants; it does not involve the rates of growth of the variables under consideration. Eq. (8) is, of course, identical with the earlier model given by Eq. (4) since it can be rewritten as

$$X = A_2(Y)^{B_2}$$
 where $A_2 = \frac{K_2}{K_1^{\frac{1}{M}}}$, $B_2 = \frac{1}{M}$. (9)

Remark: generalization

Suppose that X and Y increase according to different forms of S-shaped curves, let

$$\frac{1}{Y}\frac{dY}{dt} = u_1(K_1 - Y)\frac{1}{X}\frac{dX}{dt} = u_2(K_2 - X^m)$$

$$b_1 \qquad b_2$$

where $u_1 = \frac{b_1}{K_1}$ and $u_2 = \frac{b_2}{K_2}$. The solution of this system of equations is given

$$\frac{1}{X}\frac{dX}{dt} = B_3 \left(\frac{1}{Y}\frac{dY}{dt}\right)$$
or $X = A_2(Y)^{B_3}$ (10)

 $^{^2}$ Briefly, I_1 is a constant, K_1 is the equilibrium level of growth, and J_1 is the rate-of-growth parameter.

where $\log A_3$ is a constant of integration and

$$B_3 = \frac{1}{m}$$
 $m = \frac{K_1 u_1}{K_2 u_2}$ $A_3 = \left(\frac{K_2}{K_1}\right)^{\frac{1}{m}}$.

Clearly, the form of the Eq. [10] is identical with that of Eq. (4) and (9).

2. Application: Measuring the morphological change of economic growth

The application of the model above is based on Italy. This study uses the variable: region's *i* annualized growrate of per capita Gross Domestic Product (GDP), measured in Euros (value in 2003; cf., table 1A). The source data are from ISTAT (Italian National Institute for Statistics) for the 1980-2003 period, divided into 20 regions and three macro regions (Table 1).

Table 1. Italian regions and macro regions

Abbreviations	Macro-Region	Regions
N Italy	Italy North of Italy Liguria, Lombardia, Piemonte and Valle d'Aosta; Emi	
	•	Friuli-Venezia Giulia, Trentino-Alto Adige, Veneto
C Italy	Central part of Italy	Abruzzo, Lazio, Marche, Toscana, Umbria
S Italy	South of Italy and Islands	Basilicata, Calabria, Campania, Molise, Puglia, Sardegna, and Sicilia

The study here measures and analyzes the patterns of economic growth of some Italian regions (which are not included in the North of Italy), in relation to (rich) Northern Italy. Moreover, the paper investigates the economic growth of Italian macro-regions, Centre and South of Italy, in relation to the North of Italy.

Although differences in technology, preferences, and institutions do exist across regions, these differences are likely to be smaller than those across countries. Firms and households of different regions within a single country tend to have access to similar technologies and have roughly similar tastes and cultures. Furthermore, the regions share a common central government and therefore have similar institutional setups and legal systems. This relative homogeneity means that absolute convergence is more likely to occur across regions within countries than across countries. Another consideration is that inputs tend to be more mobile across regions than across countries. Legal, cultural, linguistic, and institutional barriers to factor movements tend to be smaller across regions within a country than across countries.

The following assumptions are the basis of the model:

- 1. let S_1 = regional system 1; S_2 = regional system 2, MR=Macro region*, I assume that S_1 , S_2 , MR \subseteq A (country system), $S_1 \cap MR = \emptyset$ and $S_2 \cap MR = \emptyset$
- 2. patterns of per capita GDP grow in the short-medium run with an S-Shaped pattern (Jarne *et al.*, 2005; *see* figure 1A).
- 3. adjacent regions within a country (e.g., Italy) are homogenous in terms of groups of people, institutions and firms, investment habits, savings, consumption, social status, cultures, tastes, financial positions, open-mindedness, laws, industries, etc.
- 4. the North of Italy is a richer economic system than other Italian regions and macro-regions and it is able to promote economic growth in other regions.

Remark: Although the North of Italy is formed by the North East and North West, which have different characteristics, I assume Northern Italy to be a homogeneous system (on the whole) richer than other Italian regions.

Remark: This analysis performs comparison among homogenous elements which are sub-sets of a system; in other words, given the C_1 and C_2 country systems

and the R_1 region such that $R_1 \subseteq C_1$, we cannot measure the economic growth of R_1 in relation to C_2 because $R_1 \not\subset C_2$. (i.e., the economic growth of Italian regions cannot be compared with a German region because of differences in habits, institutions, laws, national system of innovation, etc.; therefore, we draw a comparison "within" the country).

The analysis is carried out on the matrix R=24 (years) \times 13 (regions: 12 regions+1 macro-region* of North Italy) of the Italian economic system:

```
R = \begin{bmatrix} GDP\ 1980region_{l} & .... & GDP\ 1980region_{l} & ... & GDP\ 1980region_{l2} & GDP\ 1980Macro-region* \\ ... & GDP\ year\ i/region_{l} & .... & GDP\ year\ i/region_{l2} & GDP\ year\ i/Macro-region* \\ ... & GDP\ 2003region_{l} & .... & GDP\ 2003region_{l} & ... & GDP\ 2003Macro-region* \\ \end{bmatrix}
```

and the matrix MR= 24 (years) \times 3 (Macro Regions):

```
MR = \begin{bmatrix} GDP\ 1980macro-region_1 & GDP\ 1980macro-region_2 & GDP\ 1980macro-region_3 * \\ ... \\ GDP\ year\ i\ /\ macro-region_1 & GDP\ year\ i\ /\ macro-region_2 & GDP\ year\ i\ /\ macro-region_3 * \\ ... \\ GDP\ 2003macro-region_1 & GDP\ 2003macro-region_2 & GDP\ 2003macro-region_3 * \\ \end{bmatrix}
```

Remark: Macro region* is the North of Italy, which I assume to be the engine of overall Italian economic growth; *region*; and other macro-regions are not included in the Macro region*, *i.e.* the North of Italy.

Our function of economic growth is given by:

$$y_t = a \cdot (x_t)^B$$

where:

a is a constant

 y_t is region i's annualized growth rate of GDP per capita at time t

 x_t is Northern Italy's annualized growth rate of GDP per capita at time t, such that $t \in \{1980, ..., 2003\}$, measured in Euros (2003 value).

The North of Italy is a driving force (similar to a locomotive) of the economic growth of other Italian regions (wagons) and of the overall Italian economic system.

Remark: I assume, as already said, that growth in a leading region is capable of promoting growth in other regions to a lower, similar, or higher extent.

Remark: Let b_1 and b_2 be the growth rates of the total outputs of economic systems, Y(region) and $X(North\ of\ Italy)$ respectively, so that

$$B_1 = \frac{b_1}{b_2}$$
 measures the relative economic growth of economic system Y in

relation to the economic growth of X.

The Moving Average is applied to data to smooth out the fluctuations underlying the GDP growth rate in order to eliminate the serial correlations. In particular, the moving averages are calculated over three years, instead of five years, to avoid having shorter time series for the regression analyses. These data are then transformed into natural logarithmic data before calculations are carried out to have normal distribution.

In fact, the logarithmic form of equation $y_t = a \cdot x_t^B$ is a simple linear relationship:

$$\ln y_t = \ln a + B \ln x_t + \varepsilon_t \tag{11}$$

I consider the following hypotheses:

- if the GDP per capita growth of the region represented on the y-axis is lower than the GDP per capita growth of the macro region* represented on the x-axis and B = I, both total outputs (regions and North of Italy) are growing at the same rate (*economic isometric growth of regional systems*); in this case regional economic growth follows steady-state growth (s*). This is similar to a balanced-growth path.
- if the GDP per capita growth of the region represented on the *y*-axis is lower than the GDP per capita growth of the macro region* represented on the *x*-axis and B<1, the component represented on the *y* axis (growth rate of regional GDP per capita) is growing more slowly than the component on the *x* axis (which represents the North of Italy); this hypothesis (Hp) presents a negative disproportionate (allometric) growth of the regionsin relation to the Macro region* (or under development). In other words, this generates a particular kind of unbalanced growth.
- if the GDP per capita growth of the region represented on the y-axis is lower than the GDP per capita growth of the Macro region* represented on the x-axis and B> 1, the y axis component is growing faster than the x axis component; there is a positive disproportionate (allometric) growth or economic development of the regional systems in relation to the Macro region*.

Remark. The concepts of isometric, negative, and positive disproportionate (allometric) economic growth are based on an unconditional approach, which does not consider additional variables.

Remark. If there are economic systems Ω and Θ (e.g. regions), with Ω , $\Theta \subseteq A$ (country system: e.g. Italy), represented on the *y*-axis, where Ω is a poor region and Θ a rich one (i.e., with high GDP per capita), and $X \subseteq A$, an economic system richer than Ω and Θ ; if X is represented on the *x*-axis, the patterns of economic growth of Ω towards Θ depend on parameter B of Ω and Θ respectively.

Remark. If there are several economic systems Ω_1 , Ω_2 ,..., Ω_i ,..., $\Omega_n \subseteq A$ represented on the *y*-axis, with different starting situations represented by GDP per capita, and $X\subseteq A$, a rich economic system, if X (represented on *x*-axis) is the engine of the economic growth of the overall system A, this model shows the patterns of economic growth of these economic systems $\Omega_i(i=1,...n)$ in relation to each other regions and to the rich economic region X.

To sum up, the cases analyzed in this study are the Italian regions and two macro-regions over 24-year time series. As the patterns of economic growth of Italian regions and macro regions in the period 1980-2003 are S-shaped functions (see figure 1A in the Appendix), I apply model (11).

The model (11) has linear parameters that are estimated by the Ordinary Least-Squares Method. The calculation is carried out using the SPSS statistics software. Table 2 presents the typology of economic growth of regions and macro-regions in relation to the North of Italy.

Table 2. Typology of economic growth of Italian regions and macro-regions (period 1980-2003)

Regions	\hat{B}_1 (Std. Err.)	Typology of economic growth with sig. 5%	R ² Adjusted	
Sardegna	0.582* (0.230)	ALLOMETRY –	0.213	
Marche	0.697** (0.102)	ALLOMETRY –	0.684	
Campania	0.798# (0.340)	suspect Allometry –	0.184	
Basilicata	0.294** (0.224)	ALLOMETRY –	0.036	
Puglia	1.027# (0.156)	suspect Allometry +	0.689	
Molise	0.793* (0.069)	ALLOMETRY –	0.855	
Lazio	0.755# (0.170)	suspect isometry	0.472	
Calabria	0.357** (0.108)	ALLOMETRY –	0.321	
Abruzzo	0.628** (0.110)	ALLOMETRY –	0.622	
Umbria	0.618# (0.122)	suspect isometry	0.533	
Toscana	0.651** (0.083)	ALLOMETRY –	0.744	
Sicilia	0.261** (0.100)	ALLOMETRY –	0.234	
Macro-Regions				
C Italy	0.630** (0.056)	ALLOMETRY –	0.857	
S Italy	<i>0.927#</i> (0.105)	suspect isometry	0.778	

Note: * Level of significance 5% ** Level of significance 1‰ # A non-significant B means that there is no (significant) relationship between the growth rate of the region under investigation and Northern Italy. Statistical inference on regression coefficients indicates suspect isometry or negative/positive disproportionate (allometric) growth: the Null Hypothesis is $H_0: \hat{B} = 1$

The parametric estimates are presented in Tables 2A-3A (in the Appendix).³ Firstly, in a few cases the results from the Durbin-Watson (DW) test indicate the presence of serial correlation in the residuals of the equations. In the other cases, however, the DW's *d* statistic is in the zone of indeterminacy and of acceptance of the null hypothesis. The parametric estimates of the models are unbiased, the *t*-test presents significance of the coefficients at 1‰ and 5%, and the R² values are high, except for a few cases. Thus, in the majority of cases the models explain more than 50% of variance in the data. The results reveal (with 5% level of significance) that eight regions have negative disproportionate (allometric) economic growth; moreover, there is one suspect negative allometry (Campania), two suspect isometric growth (Lazio and Umbria) and one suspect positive allometry or economic development (Puglia). These results are due to a non-significant B in the regression analysis, even if the *t*-test B=1 provides for acceptance or rejection of the null hypothesis.

The relative changes in the economic growth of two macro-regions in relation to the growth rate of the North of Italy suggest that there is a (suspect) isometric economic growth of the South of Italy (coefficient 0.93) and a negative economic allometry for the central part of Italy in relation to the North of Italy over the 1980-2003 period. The functions of economic growth of these two Italian macro-regions are:

$$CITALYy_{t} = 0.603 \cdot NITALY x_{t}^{0.63}$$

³ To reduce the autocorrelation of Calabria, Lazio, Toscana and the central part of Italy, these areas are standardized to the 1981 value, while Sardegna and Umbria to the 2003 value.

(C Italy with *negative* disproportionate – allometric –economic growth)

$$SITALYy_t = 1.135 \cdot NITALY x_t^{0.93}$$

(S Italy with suspect "isometric" economic growth)

Therefore, this model suggests three behaviours (Figure 1):

- *Economic isometric growth* (suspect) of the regional system if both growth rates of GDP per capita (regions and North of Italy) are growing at the same rate.
- Economic development of the regional system if the regional growth rate of GDP per capita is growing faster than the growth rate of GDP per capita in the North of Italy.
- Negative economic disproportionate (allometric) growth of the regional system if the growth rate of the GDP per capita is growing more slowly than the growth rate of GDP per capita in the North of Italy.

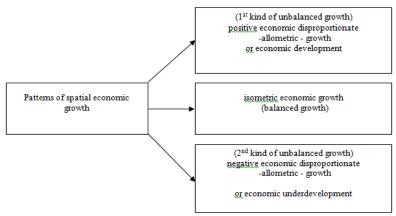


Figure 1. Patterns of spatial economic growth

The results are summarized in table 2 above, whereas figure 2 shows the magnitude (speed) of regional economic growth; Figures 3 and 4 reveal the spatial morphology of Italian regional economic growth.

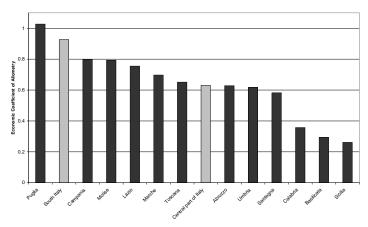


Figure 2. Magnitude (speed) of the economic growth rate of Italian regions in comparison with the North of Italy, using allometric coefficients



Figure 3. Patterns of spatial economic growth within Italian regions (1980-2003 period) in comparison with the North of Italy, considering the 5% significance

Note: Some regions have a non-significant B₁, *i.e.* there is no (significant) relationship between the growth rate of the region under investigation and Northern Italy. However, statistical inference on regression coefficients indicates suspect patterns of regional economic growth: # Suspect isometric growth in Lazio, Umbria; \$suspect negative *disproportionate (allometric)* growth in Campania, and \$ suspect positive *disproportionate (allometric)* growth in Puglia.



Figure 4. Patterns of spatial economic growth of Italian macro-regions (1980-2003 period) in comparison with the North of Italy, considering the 1‰ significance

Note: The # macro-region has a non-significant B₁, i.e. there is no (significant) relationship between the growth rate of the region under investigation and Northern Italy. Statistical inference on regression coefficients indicates suspect isometry in the South of Italy.

Finally, relative changes in economic growth of some regions are represented by the following functions:

 $\begin{aligned} \textit{Pugliay}_t &= 0.975 \cdot \textit{NITALY} \ x_t^{1.028} \\ &(\text{suspect positive disproportionate} - \text{allometric} - \text{economic growth}) \\ &\textit{Campaniay}_t = 1.185 \cdot \textit{NITALY} \ x_t^{0.798} \\ &(\text{suspect isometric economic growth}) \end{aligned}$

 $Toscanay_t = 0.075 \cdot NITALY x_t^{0.651}$

(negative disproportionate – allometric –economic growth; i.e., under development)

Appendix

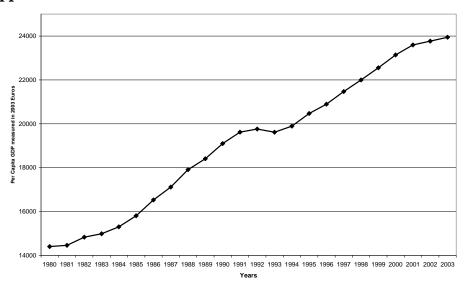


Figure 1A . *S-shaped economic growth pattern of Central Italy* **Note:** This pattern of economic growth is similar in the North Italy, South Italy and other regions

Table 1A. GDP per capita of Italian regions and macro regions in 1981, 1991 and 2001; GDP in millions of Euros, measured in 2003 value

		GDP PER CAPITA		
	Regions	1981	1991	2001
	Piemonte	16,439	21,645	25,871
North of Italy	Valle d'Aosta	19,826	27,509	28,564
	Lombardia	17,925	25,136	28,724
	Liguria	14,070	20,272	24,818
	Trentino-Alto Adige	17,861	25,942	29,120
	Veneto	15,364	21,509	25,503
	Friuli-Venezia Giulia	13,933	20,213	25,117
	Emilia-Romagna	18,032	23,491	28,084
	Toscana	15,604	20,400	24,852
	Umbria	13,881	18,357	21,736
Ct1t - £It-1	Marche	13,974	18,331	22,381
Central part of Italy	Lazio	14,371	21,379	25,411
	Abruzzo	11,507	17,190	19,110
	Molise	9,895	14,337	17,372
	Campania	8,958	12,536	14,873
	Puglia	9,101	12,746	14,950
C41 C14-1	Basilicata	8,917	11,971	15,514
South of Italy	Calabria	8,131	11,437	13,955
	Sicilia	9,859	13,682	15,040
	Sardegna	10,304	14,630	17,053
	Italy	13,782	19,039	22,438
	Italy North West	17,048	23,604	27,509
	Italy North East	16,418	22,488	26,746
Macro regions	Italy Central part	14,691	20,438	24,544
	Italy South	9,123	12,869	15,232
	Islands	9,968	13,916	15,538

Table 2A. Parametric estimates of allometric economic growth model, regions in the 1980-2004 period

2004 penoa				
Regions	Estimated relationship			
lnAbruzzoy _t =	$0.406 + 0.628 \ln NItaly X_t$	R ² adj=0.622	F=32.25 (sig.0.00)	DW=0.978
N=20	(0.131) (0.110)	S=0.525		
lnBasilicatay _t =	0.669 $+ 0.294 \ln NItaly X_t$	R² adj=0.036	F=1.716 (sig. 0.21)	DW=0.994
N=20	(0.231) (0.224)	S=0.789		
lnCalabriay,=	$-2.027 + 0.357 \ln NItaly X_t$	R² adj=0.321	F=10.927(sig. 0.04)	DW=2.207
N=22	(0.386) (0.108)	S=0.419		
InCampaniay _i =	$0.170 + 0.798 \ln NItaly X_t$	R^2 adj=0.184	F=5.518 (sig.0.03)	DW=1.436
N=21	(0.395) (0.340)	S=1.643	, ,	
InLazioy,=	$-2.742 + 0.755 \ln NItaly X_t$	R^2 adj=0.472	F=19.773(sig. 0.00)	DW=0.867
N=22	(0.606) (0.170)	S=0.658		
InMarchey,=	$0.215 + 0.697 \ln NItaly X_t$	R^2 adj=0.684	F=46.510 (sig. 0.00)	DW=0.392
N=22	(0.102) (0.102)	S=0.396		
$lnMolisey_t =$	0.353 $+ 0.793 \ln NItaly x_t$	R^2 adj=0.855	F=130.471 (sig. 0.00)	DW=1.331
N=23	(0.080) (0.069)	S=0.358		
InPugliay _i =	$-0.025 + 1.028 \ln NItaly X_t$	R² adj=0.689	F=43.124 (sig. 0.00)	DW=1.805
N=20	(0.156) (0.156)	S=0.498		
InSardegnay,=	$-0.295 + 0.582 \ln NItaly x_t$	R ² adj=0.213	F=6.407 (sig. 0.02)	DW=0.932
N=21	(0.298) (0.230)	S=0.862		
lnSiciliay _i =	$0.735 + 0.261 lnNItaly X_t$	R^2 adj=0.234	F=6.780 (sig. 0.02)	DW=1.289
N=20	(0.118) (0.100)	S=0.482	, ,	
InToscanay,=	$-2.590 + 0.651 \ln NItaly x_t$	R ² adj=0.744	F=62.017(sig. 0.00)	DW=1.973
N=22	(0.295) (0.083)	S=0.320		
$lnUmbriay_t =$	$0.534 + 0.618 \text{ lnNItaly } x_t$	R^2 adj=0.553	F=25.786 (sig. 0.00)	DW=1.019
N=21	(0.158) (0.122)	S=0.456	(2 /	

Table 3A. Parametric estimates of the economic model of allometry, macro regions in the 1980-2004 period

Macro regions	Estimated relationship				
$lnCItaly(y_t)=$					
	-0.505 $+$ 0.630	R^2 adj=0.857	F=126.990	(sig.	DW=1.170
	$lnNItaly x_t$		0.00)		
N=23	(0.200) (0.056)	S=0.217			
$lnSItaly(y_t)=$	0.127 +0.927 lnNItaly	R^2 adj=0.778	F=77.612	(sig.	DW=1.545
, ,	X_t	,	0.00)		
N=23	(0.121) (0.105)	S=0.542			

Note 1: The second column is the estimate of the constant. Given below it, in parentheses, is its standard error. The third column is the estimate of β , with below it, in parentheses, its standard error. The fourth column shows the adjusted R^2 of the regression and, below the R^2 the standard error of the regression. The fifth column displays the results of the Fisher test, to its right the significance. In the last column is the Durbin-Watson test, which is an indicator of autocorrelation of the time series.

Note 2. N=shorter time series in some regions are due to the moving average that reduces the time series by one and also to the impossibility of calculating the logarithm for some values.

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